

# Lesson 11: Interactions, Part 1

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# Learning Objectives

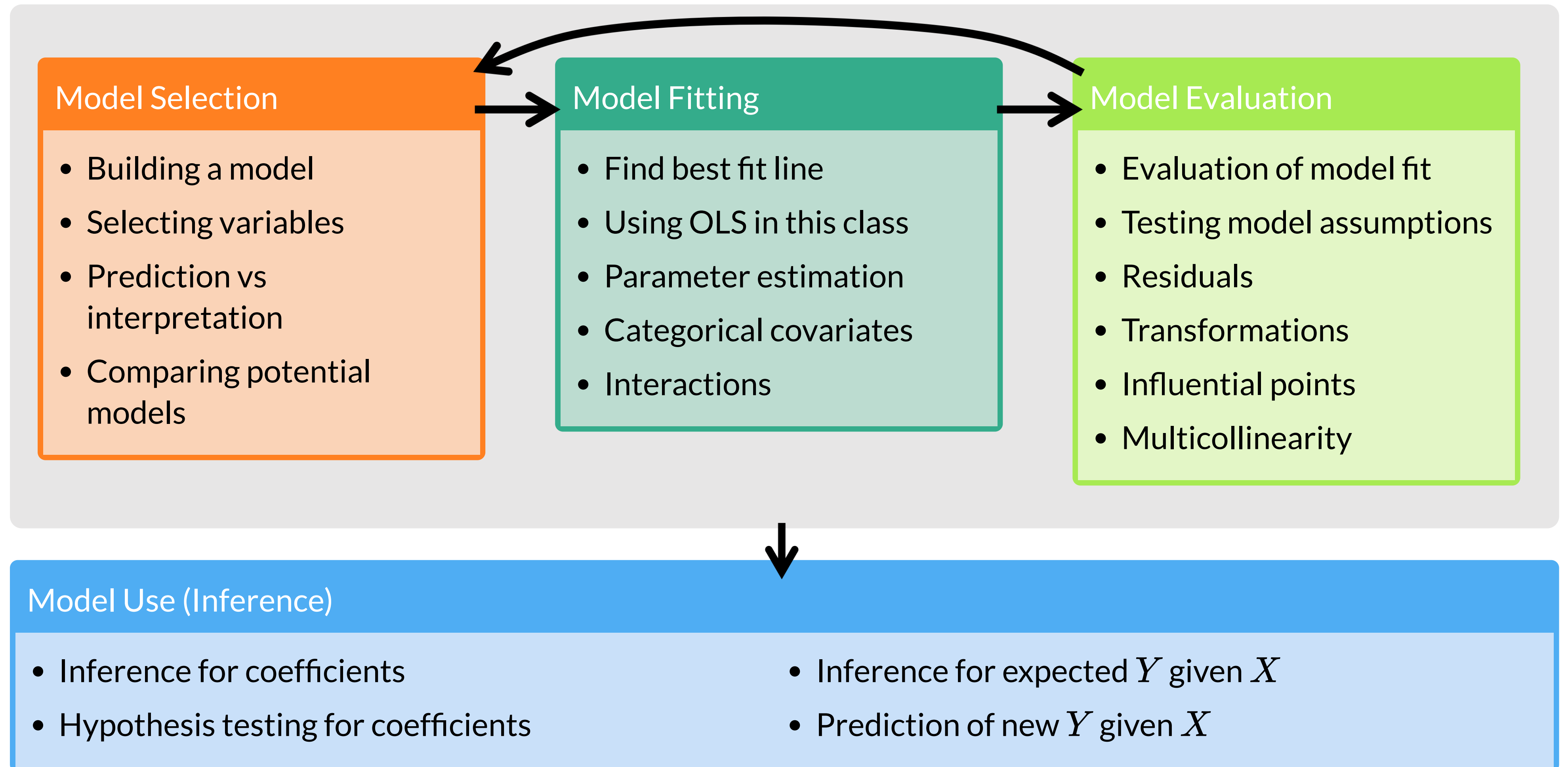
## This time:

1. Define confounders and effect modifiers, and how they interact with the main relationship we model.
2. Interpret the interaction component of a model with a **binary categorical covariate and continuous covariate**, and how the main variable's effect changes.
3. Interpret the interaction component of a model with a **multi-level categorical covariate and continuous covariate**, and how the main variable's effect changes.

## Next time:

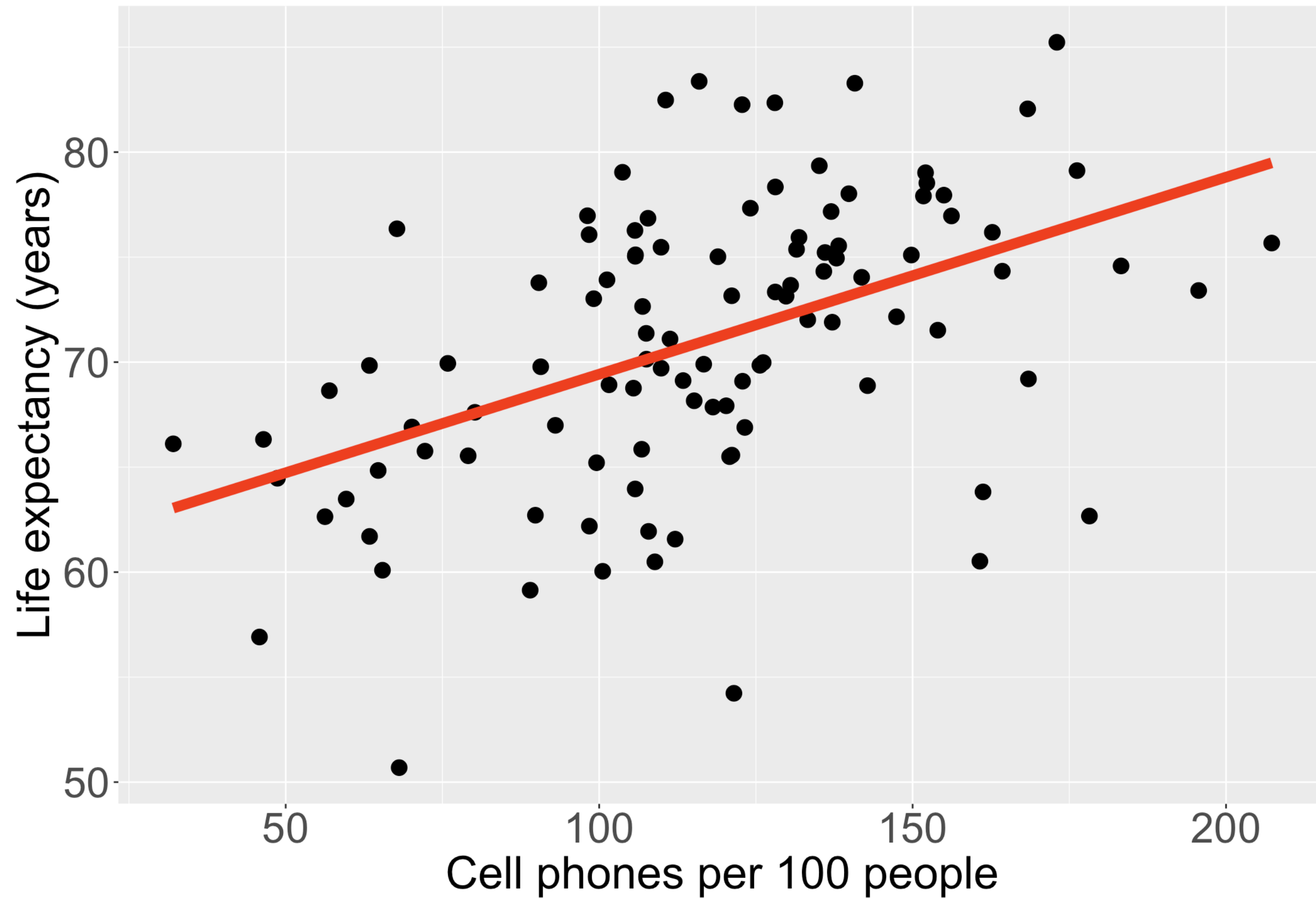
4. Interpret the interaction component of a model with **two categorical covariates**, and how the main variable's effect changes.
5. Interpret the interaction component of a model with **two continuous covariates**, and how the main variable's effect changes.

# Regression analysis process



# Recall our data and the main relationship

Relationship between life expectancy and cell phones



# Learning Objectives

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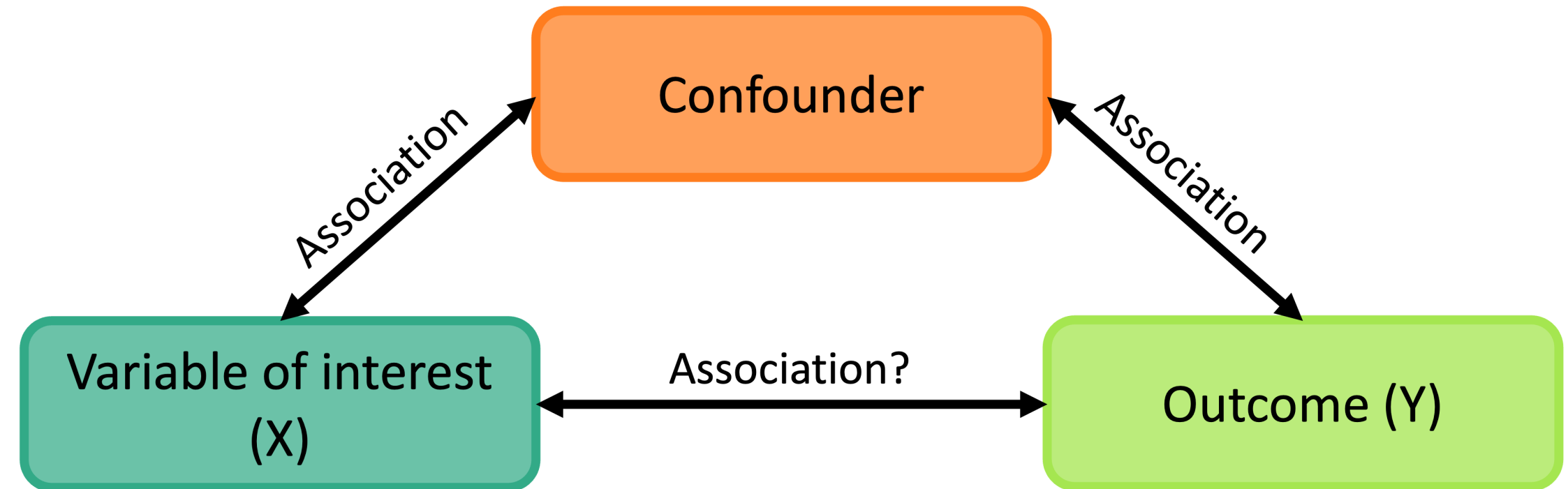
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## Next time:

4. Interpret the interaction component of a model with **two categorical covariates**, and how the main variable's effect changes.
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# What is a confounder?

- A **confounding variable**, or **confounder**, is a factor/variable that wholly or partially *accounts for the observed effect of the risk factor on the outcome*
- A confounder must be...
  - Related to the outcome Y, but not a consequence of Y
  - Related to the explanatory variable X, but not a consequence of X



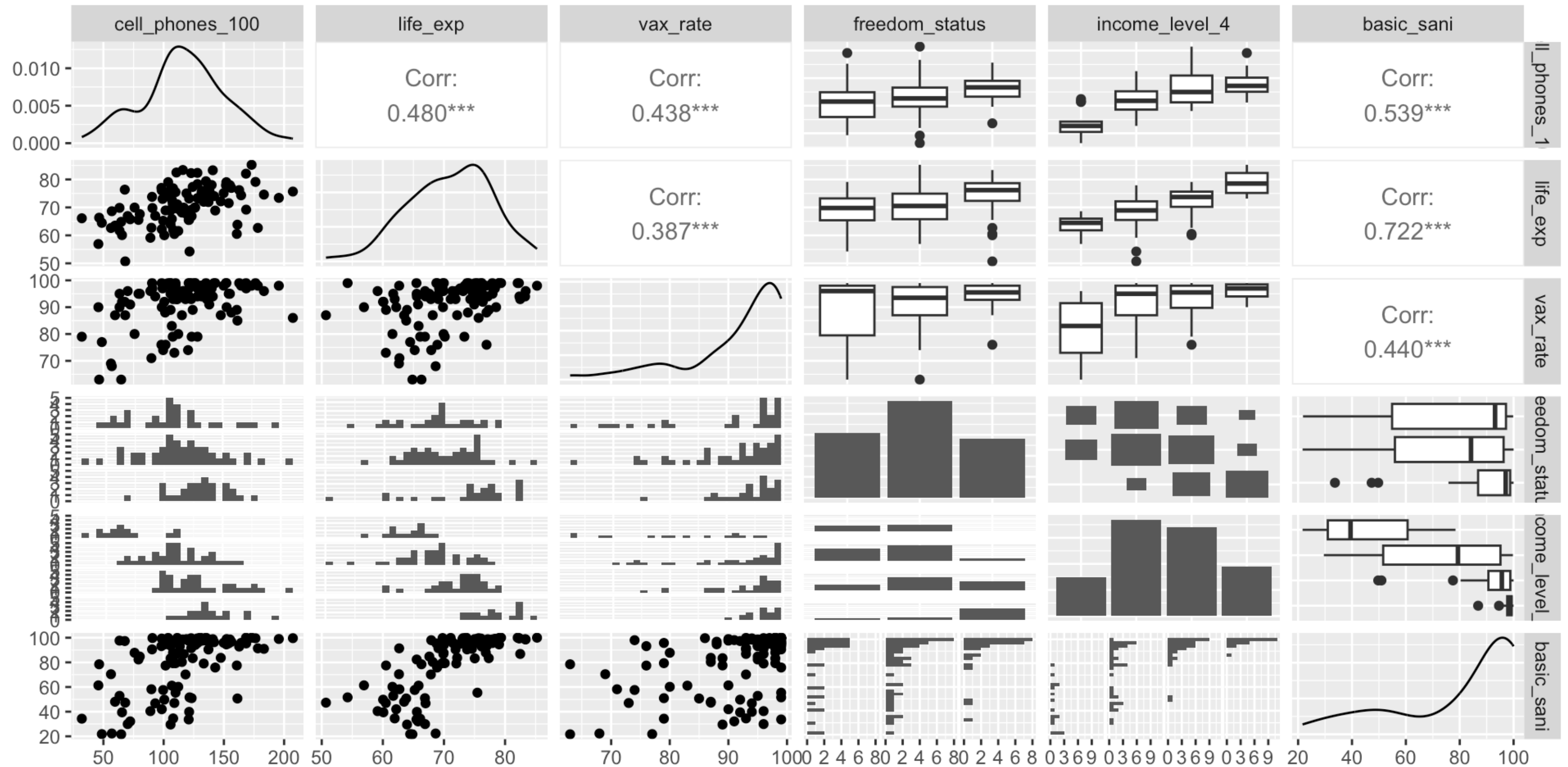
- A classic example: We found an association between ice cream consumption and sunburn!
  - If we adjust for a potential confounder, temperature/hot weather, we may see that the association between ice and sunburn is not as large
- Another example: We found an association between socioeconomic status (SES) and lung cancer!
  - If we adjust for a potential confounder, exposure to air pollution, we may see that the association between SES and lung cancer decreases

# Proxies and confounders: the good and the harmful

- *This is totally my own tangent*
- A **proxy variable** is used to stand-in or represent another variable that is harder to measure
- Sometimes a confounder can be used as a proxy if it is hard to measure you explanatory variable/variable of interest
- Proxies can be helpful statistically while harmful socially OR helpful for both!
  
- Examples
  - Bad: BMI serving as a measurement for physical health or diet
    - Many studies show how harmful, mentally and physically, it is to equate BMI to health
  - Interesting: **Using occurrence of online search queries as a proxy for public health risk perception**
  - Helpful contextualization: **Using race as a proxy for systemic racism, and thus a way to identify how to and who needs resources**
- In our lab, I discuss using sex assigned at birth in our model

# Exploratory approach to identifying confounders

```
1 gapm2 %>% ggpairs()
```



# Including a confounder in the model

- In the following model we have two variables,  $X_1$  and  $X_2$

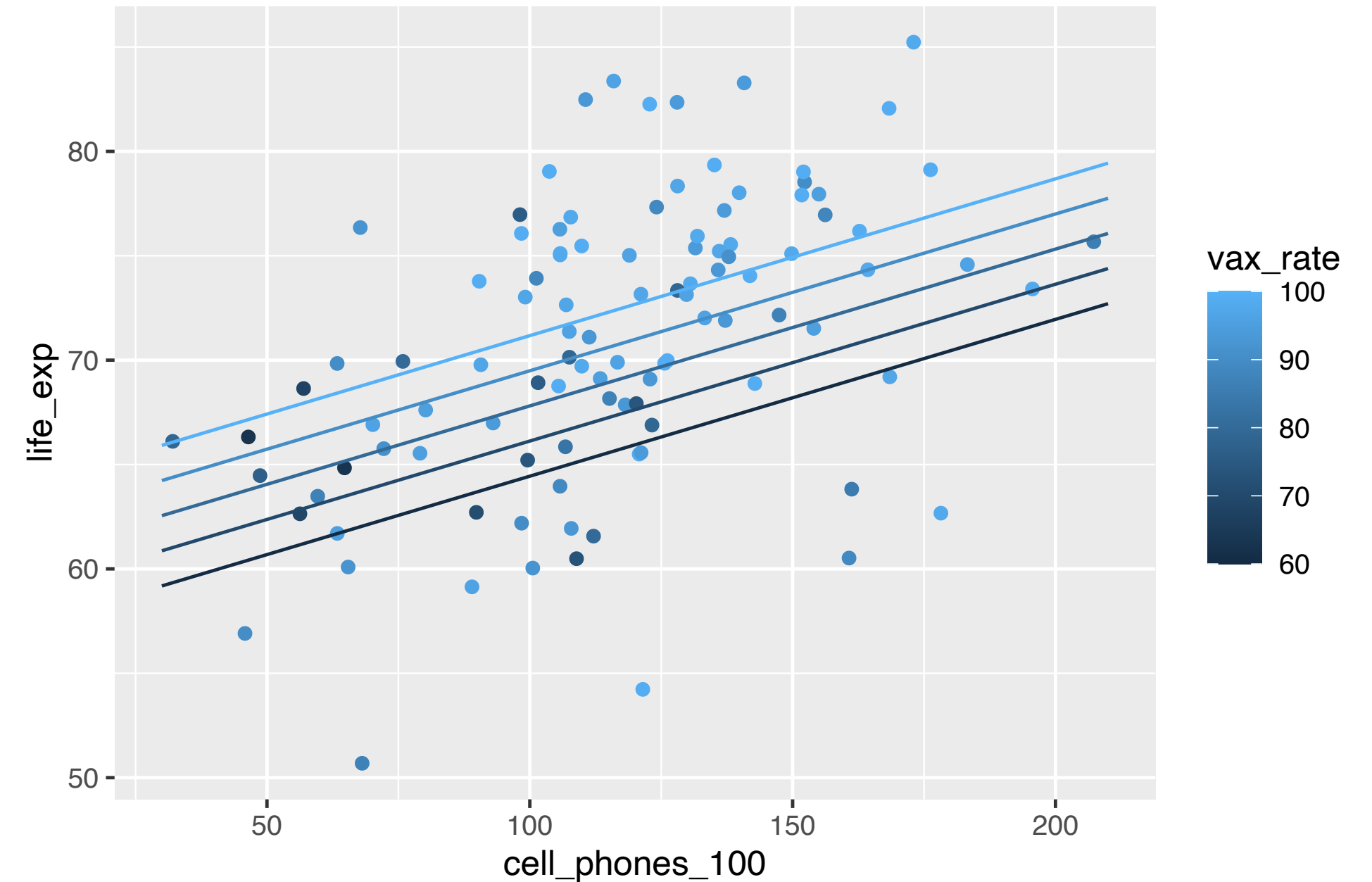
$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$$

- And we assume that every level of the confounder, there is parallel slopes
- Note: to interpret  $\beta_1$ , we did not specify any value of  $X_2$ ; only specified that it be held constant
  - Implicit assumption: effect of  $X_1$  is equal across all values of  $X_2$
- The above model assumes that  $X_1$  and  $X_2$  do not *interact* (with respect to their effect on  $Y$ )
  - Epidemiology: no “effect modification”
  - Meaning the effect of  $X_1$  is the same regardless of the values of  $X_2$
  - This model is often called a “**main effects model**”

# Where have we modeled a confounder before?

- We have seen a plot of life expectancy vs. cell phones with different levels of food supply colored (Lesson 8)
- In our plot and the model, we treat food supply as a **confounder**
- If food supply is a confounder in the relationship between life expectancy and cell phones, then we only use main effects in the model:

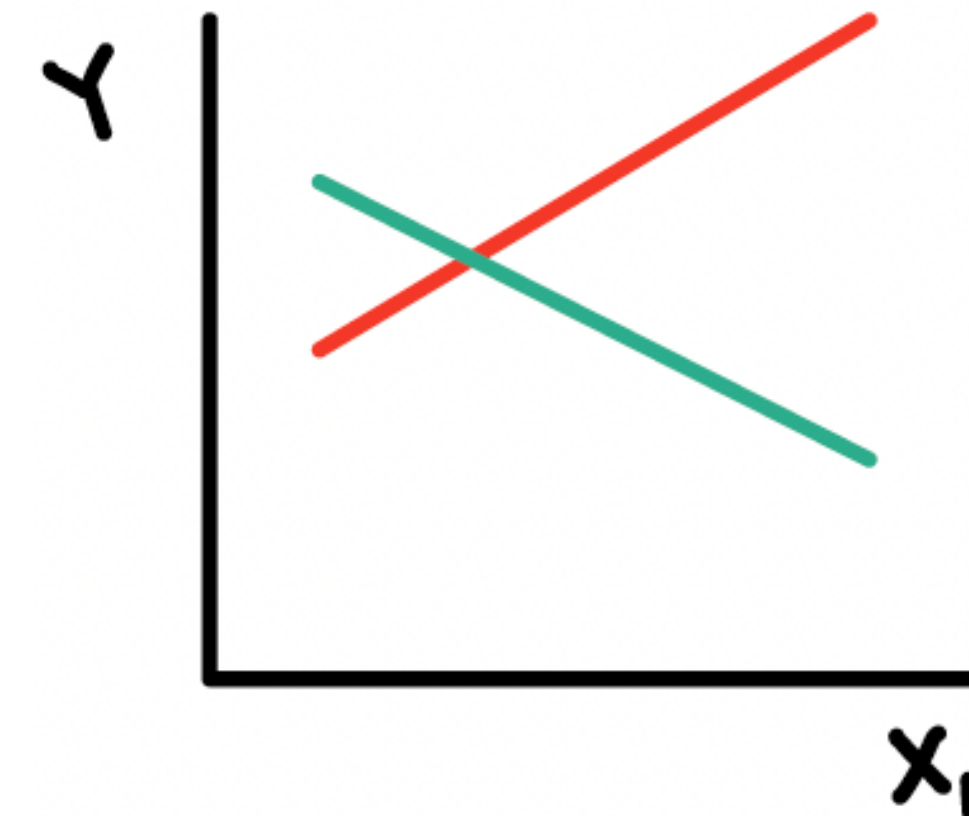
$$LE = \beta_0 + \beta_1 CP + \beta_2 VR + \epsilon$$



# Poll everywhere question 1

# What is an effect modifier?

- An additional variable in the model
  - Outside of the main relationship between  $Y$  and  $X_1$  that we are studying
- An effect modifier will change the effect of  $X_1$  on  $Y$  depending on its value
  - Aka: as the effect modifier's values change, so does the association between  $Y$  and  $X_1$
  - So the coefficient estimating the relationship between  $Y$  and  $X_1$  changes with another variable
- **Example:** A breast cancer education program (the exposure) that is much more effective in reducing breast cancer (outcome) in rural areas than urban areas.
  - Location (rural vs. urban) is the EMM



# How do we include an effect modifier in the model?

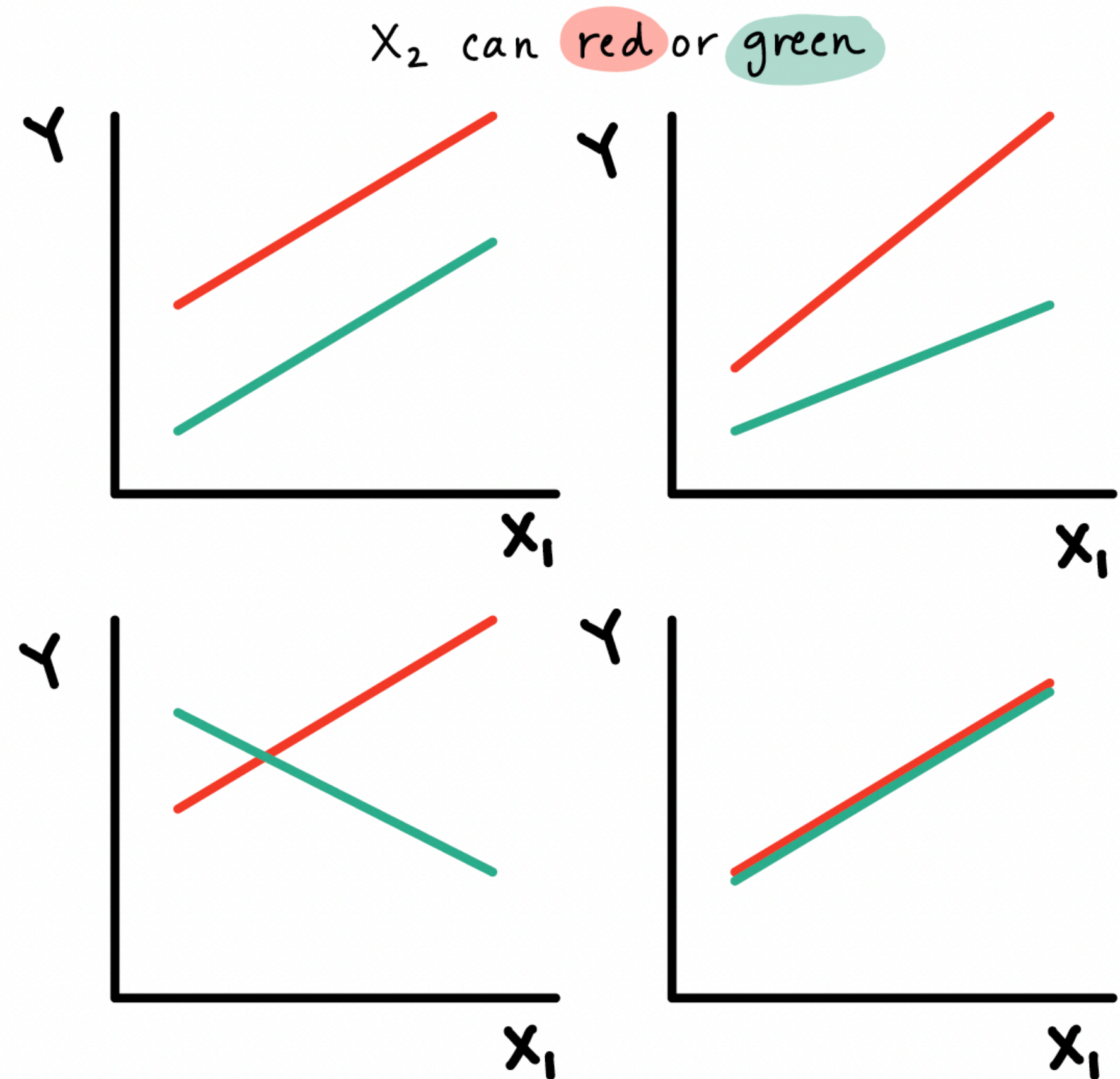
- Interactions!!
- We can incorporate interactions into our model through product terms:

$$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_1 X_2 + \epsilon$$

- Terminology:
  - main effect parameters:  $\beta_1, \beta_2$ 
    - The main effect models estimate the *average*  $X_1$  and  $X_2$  effects
  - interaction parameter:  $\beta_3$

# Types of interactions / non-interactions

- Common types of interactions:
  - Synergism:  $X_2$  strengthens the  $X_1$  effect
  - Antagonism:  $X_2$  weakens the  $X_1$  effect
- If the interaction coefficient is not significant
  - No evidence of effect modification, i.e., the effect of  $X_1$  does not vary with  $X_2$
- If the main effect of  $X_2$  is also not significant
  - No evidence that  $X_2$  is a confounder



# Learning Objectives

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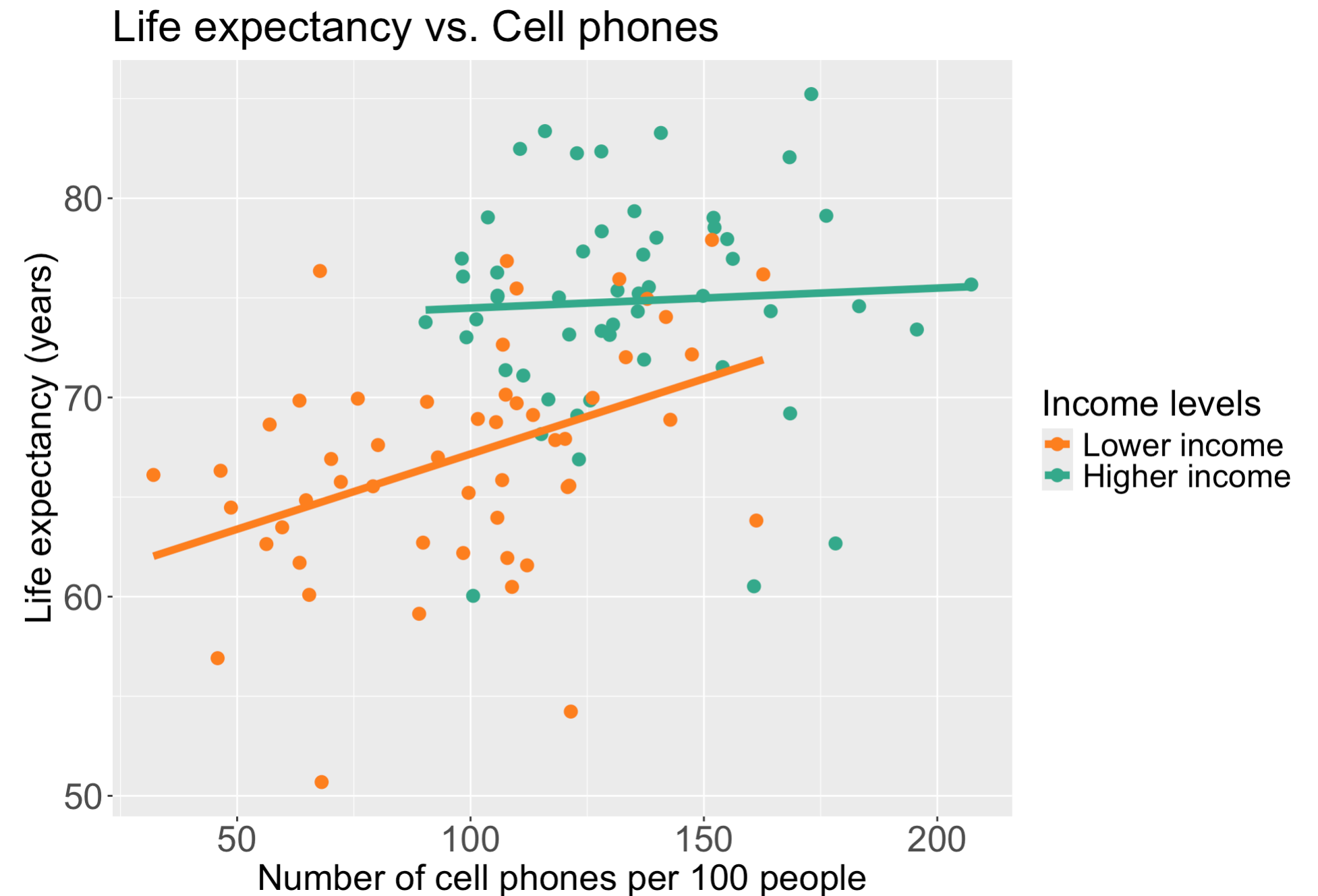
## Next time:

4. Interpret the interaction component of a model with **two categorical covariates**, and how the main variable's effect changes.

5. Interpret the interaction component of a model with **two continuous covariates**, and how the main variable's effect changes.

# Do we think income level is an effect modifier for cell phones?

- Let's say we only have two income groups: low income and high income
- We can start by visualizing the relationship between life expectancy and cell phones *by income level*
- Questions of interest: Is the effect of number of cell phones on life expectancy differ depending on income level?
  - This is the same as: Is income level is an effect modifier for cell phones?
  - “effect of cell phones” differing = different slopes between CP and LE depending on the income group
- Let's run an interaction model to see!



# Model with interaction between a *binary categorical and continuous variables*

Model we are fitting:

$$LE = \beta_0 + \beta_1 CP + \beta_2 I(\text{high income}) + \beta_3 CP \cdot I(\text{high income}) + \epsilon$$

- $LE$  as outcome
- $CP$  as continuous variable that is our main variable of interest
- $I(\text{high income})$  as the indicator that income level is “high income” (binary categorical variable)

```
1 m_int_inc2 = gapm %>%  
2   lm(formula = life_exp ~ cell_phones_100 + income_level_2 +  
3     cell_phones_100*income_level_2)
```

OR

```
1 m_int_inc2 = gapm %>%  
2   lm(formula = life_exp ~ cell_phones_100*income_level_2)
```

# Displaying the regression table and writing fitted regression equation

- ▶ Code to display regression table with interaction

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	59.609	2.406	24.776	0.000	54.836	64.382
cell_phones_100	0.076	0.023	3.247	0.002	0.029	0.122
income_level_2Higher income	13.879	4.438	3.127	0.002	5.075	22.683
cell_phones_100:income_level_2Higher income	-0.066	0.036	-1.829	0.070	-0.137	0.006

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP + \hat{\beta}_2 I(\text{high income}) + \hat{\beta}_3 CP \cdot I(\text{high income})$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP + 13.879 \cdot I(\text{high income}) - 0.066 \cdot CP \cdot I(\text{high income})$$

# Poll Everywhere Question 2

# Comparing fitted regression lines for each income level

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP + \widehat{\beta}_2 I(\text{high income}) + \widehat{\beta}_3 CP \cdot I(\text{high income})$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP + 13.879 \cdot I(\text{high income}) - 0.066 \cdot CP \cdot I(\text{high income})$$

For lower income countries:  $I(\text{high income}) = 0$

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP + \widehat{\beta}_2 \cdot 0 + \widehat{\beta}_3 CP \cdot 0$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP + 13.879 \cdot 0 - 0.066 \cdot CP \cdot 0$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP$$

For higher income countries:  $I(\text{high income}) = 1$

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP + \widehat{\beta}_2 \cdot 1 + \widehat{\beta}_3 CP \cdot 1$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP + 13.879 \cdot 1 - 0.066 CP \cdot 1$$

$$\widehat{LE} = (59.61 + 13.879) + (0.076 - 0.066) \cdot CP$$

$$\widehat{LE} = 73.49 + 0.01 \cdot CP$$

# Let's take a look back at the plot

For lower income countries:  $I(\text{high income}) = 0$

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP$$

$$\widehat{LE} = 59.61 + 0.076 \cdot CP$$

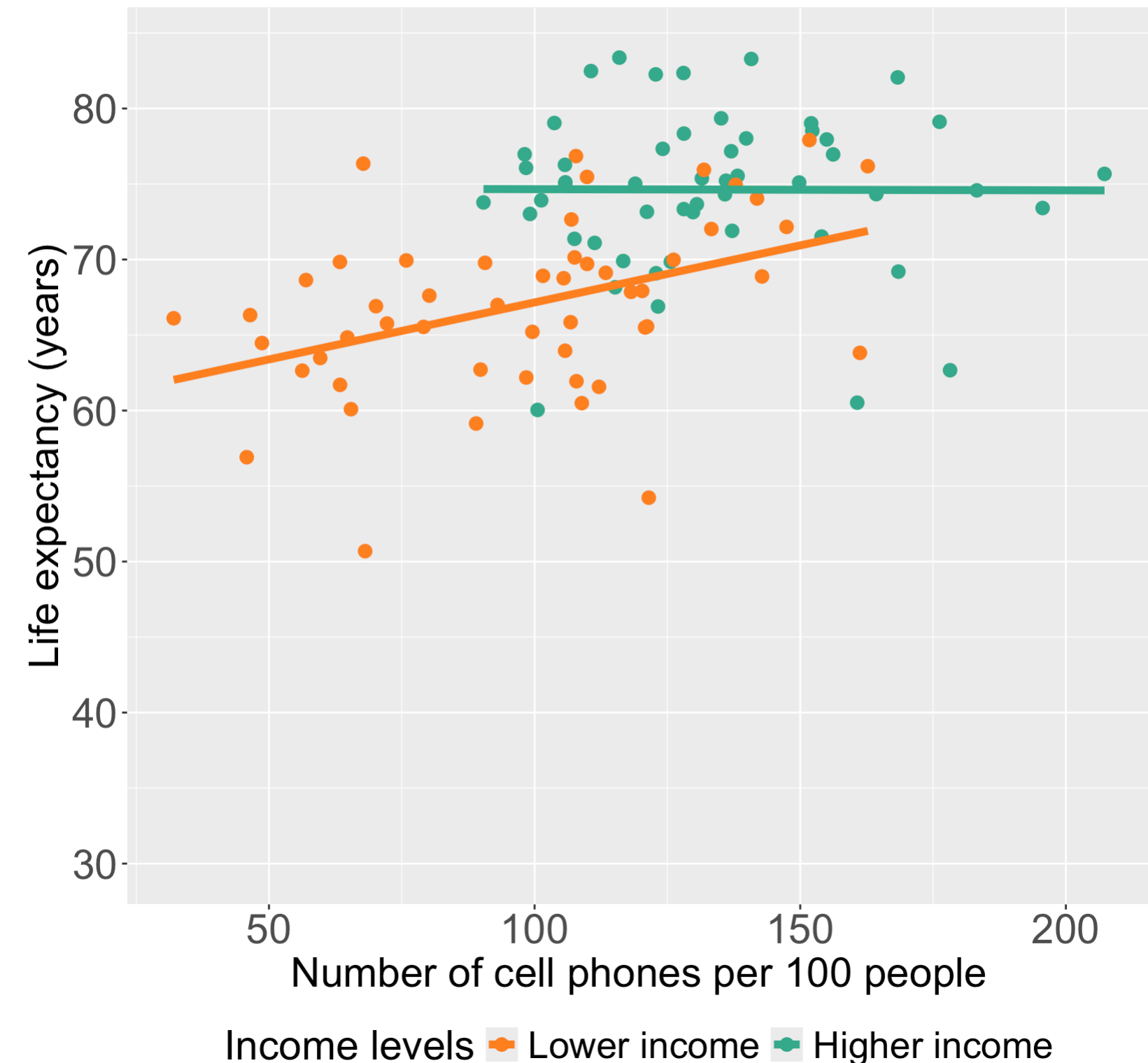
For higher income countries:  $I(\text{high income}) = 1$

$$\widehat{LE} = (\widehat{\beta}_0 + \widehat{\beta}_2) + (\widehat{\beta}_1 + \widehat{\beta}_3) CP$$

$$\widehat{LE} = (59.61 + 13.879) + (0.076 - 0.066) \cdot CP$$

$$\widehat{LE} = 73.49 + 0.01 \cdot CP$$

Life expectancy vs. Number of Cell Phones



# Poll Everywhere Question 3

# PAUSE: Centering continuous variables when including interactions

- For the high income group, the mean life expectancy had a regression line with a small intercept

$$\widehat{LE} = (\hat{\beta}_0 + \hat{\beta}_2) + (\hat{\beta}_1 + \hat{\beta}_3)CP$$

$$\widehat{LE} = (59.61 + 13.879) + (0.076 - 0.066) \cdot CP$$

$$\widehat{LE} = 73.49 + 0.01 \cdot CP$$

- Intercept of 73.49 is misleading because
  - Makes you think some of the life expectancies for high income countries are lower than that of low income countries (depending on the CP)
  - There are no high income countries with CP less than ~80
- Other online sources about when and when not to center:
  - **The why and when of centering continuous predictors in regression modeling**
  - **When not to center a predictor variable in regression**



# Centering a variable

- Centering a variable means that we will subtract the mean or median (or other measurement of center) from the measured value
- Mean centered:

$$X_i^c = X_i - \bar{X}$$

- Median centered:

$$X_i^c = X_i - \text{median } X$$

- Centering the continuous variables in a model (when they are involved in interactions) helps with:
  - Interpretations of the coefficient estimates
  - Correlation between the main effect for the variable and the interaction that it is involved with
    - To be discussed in future lecture: leads to multicollinearity issues



# It'll be helpful to center number of cell phones

- Centering number of cell phones:

$$CP^c = CP - \overline{CP}$$

- Centering in R:

```
1 gapm = gapm %>%  
2   mutate(CP_c = cell_phones_100 - median(cell_phones_100))
```

- I'm going to print the mean so I can use it for my interpretations

```
1 (mean_CP = mean(gapm$cell_phones_100))
```

```
[1] 116.5234
```

- Now all intercept values (in each respective freedom status) will be the mean life expectancy when number of cell phones per 100 people is 116.52
- We will use center CP for the rest of the lecture



# Displaying the regression table and writing fitted regression equation AGAIN

```
1 m_int_inc2 = gapm %>%  
2   lm(formula = life_exp ~ CP_c*income_level_2)
```

► Code to display regression table with interaction

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	68.420	0.851	80.361	0.000	66.731	70.109
CP_c	0.076	0.023	3.247	0.002	0.029	0.122
income_level_2Higher income	6.236	1.220	5.111	0.000	3.816	8.657
CP_c:income_level_2Higher income	-0.066	0.036	-1.829	0.070	-0.137	0.006

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 I(\text{high income}) + \hat{\beta}_3 CP^c \cdot I(\text{high income})$$

$$\widehat{LE} = 68.42 + 0.076 \cdot CP^c + 6.236 \cdot I(\text{high income}) - 0.066 \cdot CP^c \cdot I(\text{high income})$$

# Interpretation for interaction between binary categorical and continuous variables

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP^c + \widehat{\beta}_2 I(\text{high income}) + \widehat{\beta}_3 CP^c \cdot I(\text{high income})$$
$$\widehat{LE} = \left[ \widehat{\beta}_0 + \widehat{\beta}_2 \cdot I(\text{high income}) \right] + \underbrace{\left[ \widehat{\beta}_1 + \widehat{\beta}_3 \cdot I(\text{high income}) \right]}_{\text{CP's effect}} CP^c$$

- Interpretation:
  - $\beta_3$  = mean change in number of cell phones's effect, comparing higher income to lower income levels
    - AKA: the change in slopes (for line between CP and LE) comparing high income to low income
  - where the “number of cell phones effect” = change in mean life expectancy per one additional cell phone (slope) with income level held constant, i.e. “adjusted number of cell phones effect”
- In summary, the interaction term can be interpreted as “difference in adjusted cell phones' effect comparing higher income to lower income levels”
- It will be helpful to test the interaction to round out this interpretation!!

# Poll Everywhere Question 4

# Test interaction between binary categorical and continuous variables

- We run an F-test for a single coefficient ( $\beta_3$ ) in the below model (see Lesson 10, MLR: Using the F-test)

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{high income}) + \beta_3 CP^c \cdot I(\text{high income}) + \epsilon$$

Null  $H_0$

$$\beta_3 = 0$$

Alternative  $H_1$

$$\beta_3 \neq 0$$

Null / Smaller / Reduced model

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{high income}) + \epsilon$$

Alternative / Larger / Full model

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{high income}) + \beta_3 CP^c \cdot I(\text{high income}) + \epsilon$$

- I'm going to be skipping steps so please look back at Lesson 10 for full steps (required in HW 4)

# Test interaction between binary categorical and continuous variables

- Fit the reduced and full model

```
1 m_int_inc_red = gapm %>% lm(formula = life_exp ~ CP_c + income_level_2)
2 m_int_inc_full = gapm %>%
3   lm(formula = life_exp ~ CP_c + income_level_2 + CP_c*income_level_2)
```

- ▶ Code to display ANOVA table for testing interaction

term	df.residual	rss	df	sumsq	statistic	p.value
life_exp ~ CP_c + income_level_2	102.000	2,957.645	NA	NA	NA	NA
life_exp ~ CP_c + income_level_2 + CP_c * income_level_2	101.000	2,862.847	1.000	94.798	3.344	0.070

- **Conclusion:** There is not a significant interaction between cell phones and income level ( $p = 0.07$ )
  - **If significant, we say more:** For higher income levels, for every one additional cell phone per 100 people, the mean life expectancy increases 0.01 years. For lower income levels, for every one additional cell phone per 100 people, the mean life expectancy increases 0.076 years. Thus, the effect of cell phones is seven times more for high income than low income levels.

# Learning Objectives

## This time:

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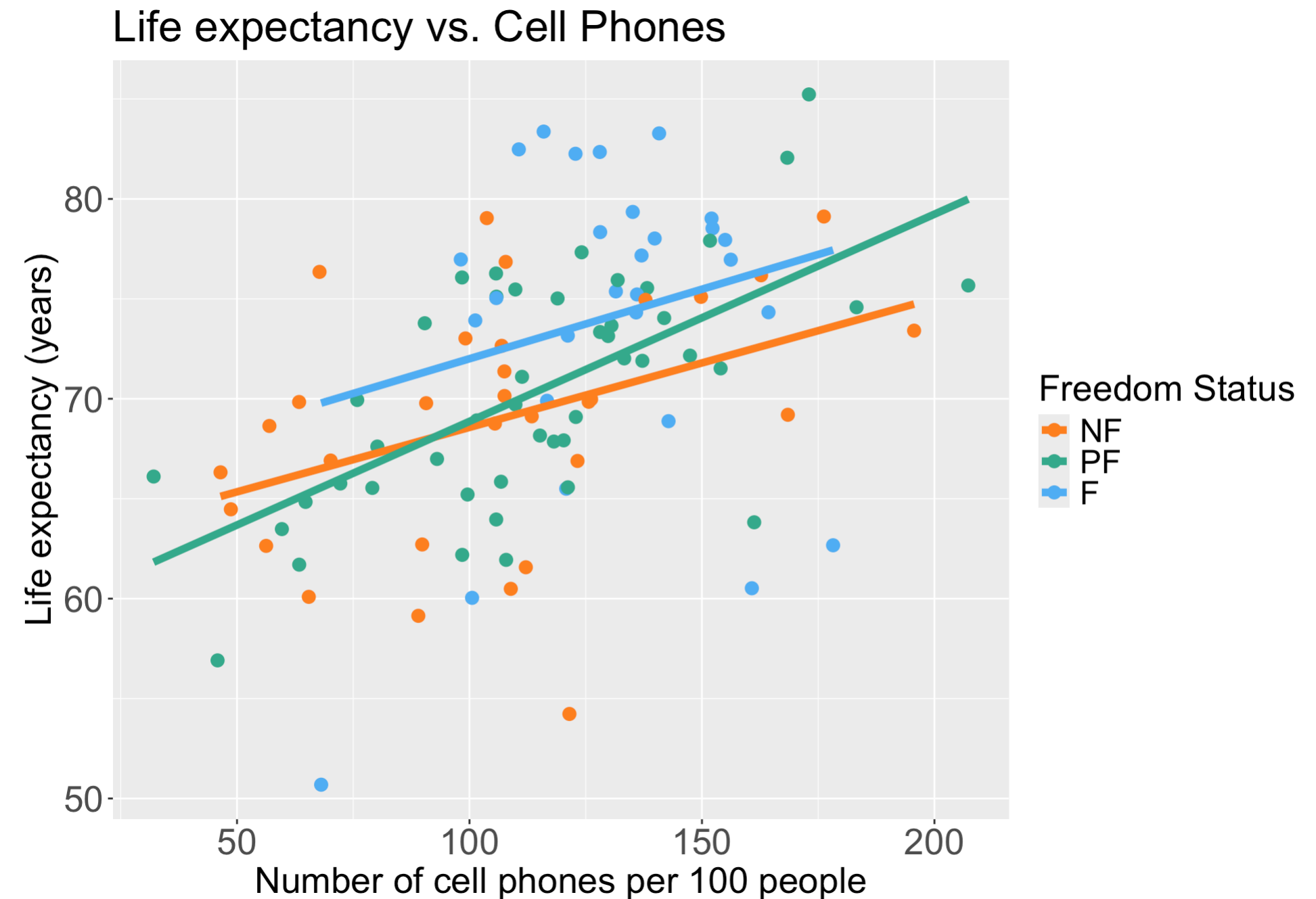
3. Interpret the interaction component of a model with a **multi-level categorical covariate and continuous covariate**, and how the main variable's effect changes.

## Next time:

4. Interpret the interaction component of a model with **two categorical covariates**, and how the main variable's effect changes.
5. Interpret the interaction component of a model with **two continuous covariates**, and how the main variable's effect changes.

# Do we think freedom status is an effect modifier for cell phones?

- We can start by visualizing the relationship between life expectancy and cell phones *by freedom status*
- Questions of interest: Does the effect of number of cell phones on life expectancy differ depending on freedom status?
  - This is the same as: Is freedom status is an effect modifier for number of cell phones?
- Let's run an interaction model to see!



# Model with interaction between a *multi-level categorical and continuous variables*

Model we are fitting:

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{FS} = \text{PF}) + \beta_3 I(\text{FS} = \text{F}) + \beta_4 CP^c \cdot I(\text{FS} = \text{PF}) + \beta_5 CP^c \cdot I(\text{FS} = \text{F}) + \epsilon$$

- $LE$  as life expectancy
- $CP^c$  as centered number of cell phones (continuous variable)
- $I(\text{FS} = \text{PF})$  and  $I(\text{FS} = \text{F})$  as the indicator for freedom status (with NF as reference group)

In R:

```
1 m_int_wr = gapm %>%  
2   lm(formula = life_exp ~ CP_c + freedom_status + CP_c*freedom_status)
```

OR

```
1 m_int_wr = gapm %>% lm(formula = life_exp ~ CP_c * freedom_status)
```

# Displaying the regression table and writing fitted regression equation

- ▶ Code to display regression table with interaction

term	estimate	std.error	statistic	p.value	conf.low	conf.high
(Intercept)	69.645	1.102	63.177	0.000	67.457	71.832
CP_c	0.065	0.029	2.263	0.026	0.008	0.121
freedom_statusPF	0.953	1.407	0.677	0.500	-1.840	3.745
freedom_statusF	3.519	1.706	2.063	0.042	0.135	6.904
CP_c:freedom_statusPF	0.039	0.038	1.036	0.303	-0.036	0.114
CP_c:freedom_statusF	0.005	0.056	0.091	0.928	-0.105	0.115

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 I(\text{FS} = \text{PF}) + \hat{\beta}_3 I(\text{FS} = \text{F}) + \\ \hat{\beta}_4 CP^c \cdot I(\text{FS} = \text{PF}) + \hat{\beta}_5 CP^c \cdot I(\text{FS} = \text{F})$$

$$\widehat{LE} = 69.645 + 0.065 \cdot CP^c + 0.953 \cdot I(\text{FS} = \text{PF}) + 3.519 \cdot I(\text{FS} = \text{F}) + \\ 0.039 \cdot CP^c \cdot I(\text{FS} = \text{PF}) + 0.005 \cdot CP^c \cdot I(\text{FS} = \text{PF})$$

# Comparing fitted regression lines for each freedom status

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 I(\text{FS} = \text{PF}) + \hat{\beta}_3 I(\text{FS} = \text{F}) + \hat{\beta}_4 CP^c \cdot I(\text{FS} = \text{PF}) + \hat{\beta}_5 CP^c \cdot I(\text{FS} = \text{F})$$

$$\widehat{LE} = 69.645 + 0.065 \cdot CP^c + 0.953 \cdot I(\text{FS} = \text{PF}) + 3.519 \cdot I(\text{FS} = \text{F}) + 0.039 \cdot CP^c \cdot I(\text{FS} = \text{PF}) + 0.005 \cdot CP^c \cdot I(\text{FS} = \text{PF})$$

Not free

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 \cdot 0 + \hat{\beta}_3 \cdot 0 + \hat{\beta}_4 CP^c \cdot 0 + \hat{\beta}_5 CP^c \cdot 0$$

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c$$

Partly free

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 \cdot 1 + \hat{\beta}_3 \cdot 0 + \hat{\beta}_4 CP^c \cdot 1 + \hat{\beta}_5 CP^c \cdot 0$$

$$\widehat{LE} = (\hat{\beta}_0 + \hat{\beta}_2) + (\hat{\beta}_1 + \hat{\beta}_4) CP^c$$

Free

$$\widehat{LE} = \hat{\beta}_0 + \hat{\beta}_1 CP^c + \hat{\beta}_2 \cdot 0 + \hat{\beta}_3 \cdot 1 + \hat{\beta}_4 CP^c \cdot 0 + \hat{\beta}_5 CP^c \cdot 1$$

$$\widehat{LE} = (\hat{\beta}_0 + \hat{\beta}_3) + (\hat{\beta}_1 + \hat{\beta}_5) CP^c$$

# Interpretation for interaction between multi-level categorical and continuous variables

$$\widehat{LE} = \widehat{\beta}_0 + \widehat{\beta}_1 CP^c + \widehat{\beta}_2 I(\text{FS} = \text{PF}) + \widehat{\beta}_3 I(\text{FS} = \text{F}) + \widehat{\beta}_4 CP^c \cdot I(\text{FS} = \text{PF}) + \widehat{\beta}_5 CP^c \cdot I(\text{FS} = \text{F})$$

$$\widehat{LE} = \left[ \widehat{\beta}_0 + \widehat{\beta}_2 I(\text{FS} = \text{PF}) + \widehat{\beta}_3 I(\text{FS} = \text{F}) \right] + \underbrace{\left[ \widehat{\beta}_1 + \widehat{\beta}_4 \cdot I(\text{FS} = \text{PF}) + \widehat{\beta}_5 \cdot I(\text{FS} = \text{F}) \right]}_{\text{CP's effect}} CP^c$$

- Interpretation:
  - $\beta_4$  = mean change in cell phones's effect, comparing countries that are partly free to countries that are not free
  - $\beta_5$  = mean change in cell phones's effect, comparing countries that are free to countries that are not free
- It will be helpful to test the interaction to round out this interpretation!!

# Test interaction between multi-level categorical & continuous variables

- We run an F-test for a group of coefficients ( $\beta_4$  and  $\beta_5$ ) in the below model

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{FS} = \text{PF}) + \beta_3 I(\text{FS} = \text{F}) + \beta_4 CP^c \cdot I(\text{FS} = \text{PF}) + \beta_5 CP^c \cdot I(\text{FS} = \text{F}) + \epsilon$$

Null  $H_0$

$$\beta_4 = \beta_5 = 0$$

Alternative  $H_1$

$$\beta_4 \neq 0 \text{ and/or } \beta_5 \neq 0$$

Null / Smaller / Reduced model

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{FS} = \text{PF}) + \beta_3 I(\text{FS} = \text{F}) + \epsilon$$

Alternative / Larger / Full model

$$LE = \beta_0 + \beta_1 CP^c + \beta_2 I(\text{FS} = \text{PF}) + \beta_3 I(\text{FS} = \text{F}) + \beta_4 CP^c \cdot I(\text{FS} = \text{PF}) + \beta_5 CP^c \cdot I(\text{FS} = \text{F}) + \epsilon$$

# Test interaction between multi-level categorical & continuous variables

- Fit the reduced and full model

```
1 m_int_fs_red = gapm %>% lm(formula = life_exp ~ CP_c + freedom_status)
2 m_int_fs_full = gapm %>%
3   lm(formula = life_exp ~ CP_c + freedom_status + CP_c*freedom_status)
```

- ▶ Code to display ANOVA table for testing interaction

term	df.residual	rss	df	sumsq	statistic	p.value
life_exp ~ CP_c + freedom_status	101.000	3,517.244	NA	NA	NA	NA
life_exp ~ CP_c + freedom_status + CP_c * freedom_status	99.000	3,475.580	2.000	41.664	0.593	0.554

- Conclusion: There is not a significant interaction between number of cell phones and freedom status (p = 0.554)
- Freedom status is NOT an effect measure modifier of CP on LE

