

# Homework 1

BSTA 550

## Directions

Please turn in [this homework on Sakai](#). Please submit your homework in pdf format. You can type your work on your computer or submit a single file with photos of your written work or any other method that can be turned into a pdf. The Adobe Scan phone app is an easy way to scan photos and compile into a PDF. Please let me know if you greatly prefer to submit a physical copy. We can work out another way for you to turn in homework.

**Try to complete all of the problems listed below at some point this quarter! You may want to save some of them for studying later!** Only turn in the ones listed in the “Turn In” column. Please submit problems in the order they are listed.

*You must show all of your work to receive credit.*

Chapter	Turn In	Extra Problems
1		# 3, 7, 9, 11
2	NTB # 1, 30	# 1, 4, 8, 16, 19, 23, NTB # 2
22*	TB # 1	# 3, 5, 7, 25, 27, 30, 31, 39-41, 43-48

\* Please note the following for Chapter 22:

- See the table on pg. 277, which summarizes some key combinatorics concepts.
- Problems 39-48 are a set that build on one another and more advanced than the other problems. It'll be much easier to do #42 after doing 39-41.
- I *highly* recommend reading Chapter 23, which is a series of case studies in counting: poker hands and Yahtzee.

## Non-textbook problems (NTB)

1. Suppose the following are the percentage of US adults with the following conditions:
  - $A$ : Hypertension 33%
  - $B$ : Diabetes 9%
  - $C$ : Metabolic syndrome 24%
  - $A$  or  $B$ : 39%
  - $A$  or  $C$ : 45%
  - $B$  or  $C$ : 28%
  - $A$  or  $B$  or  $C$ : 48%
  - a. Make a Venn diagram of the 3 conditions labeling the percentage (or probability) for *ALL* of the 8 “sections”. *Hint: Start from the last condition and work your way up!*
  - b. For each of the following (1. - 7. below), (i) write out the event using unions, intersections, and/or complements of the events  $A$ ,  $B$ , and  $C$  (this is NOT finding the probability, that’s in ii); (ii) find the probability of the event; and (iii) write a sentence explaining what the probability is of in terms of the context of the problem.
    1.  $\mathbb{P}(\text{event at least one of the 3})$
    2.  $\mathbb{P}(\text{event none})$
    3.  $\mathbb{P}(\text{event } A \text{ only})$
    4.  $\mathbb{P}(\text{event exactly one})$
    5.  $\mathbb{P}(\text{event } A \text{ and } B)$
    6.  $\mathbb{P}(\text{event } A \text{ and } B \text{ but not } C)$
    7.  $\mathbb{P}(\text{event all 3})$

## Extra problem

2. Judith has a penny, nickel, dime, and quarter in her pocket. So does Joe. They both reach into their pockets and choose a coin (all four coins are equally likely to be selected). Let  $X$  be the larger value (in cents) of the coins selected by Judith and Joe. For reference, the penny is 1 cent, nickel is 5 cents, dime is 10 cents, and quarter is 25 cents.
  - a. How many possible combinations is there for the pair of Judith’s and Joe’s selected coins? (Hint: we know to whom each coin belongs)
  - b. Define the sample space for  $X$  in this experiment.
  - c. Find the probability for each possible value of  $X$ .

- d. Find the probability of the event that Judith's coin is worth more than Joe's.