

# Lesson 12: Hypothesis Testing 1: Single-sample mean

TB sections 4.3, 5.1

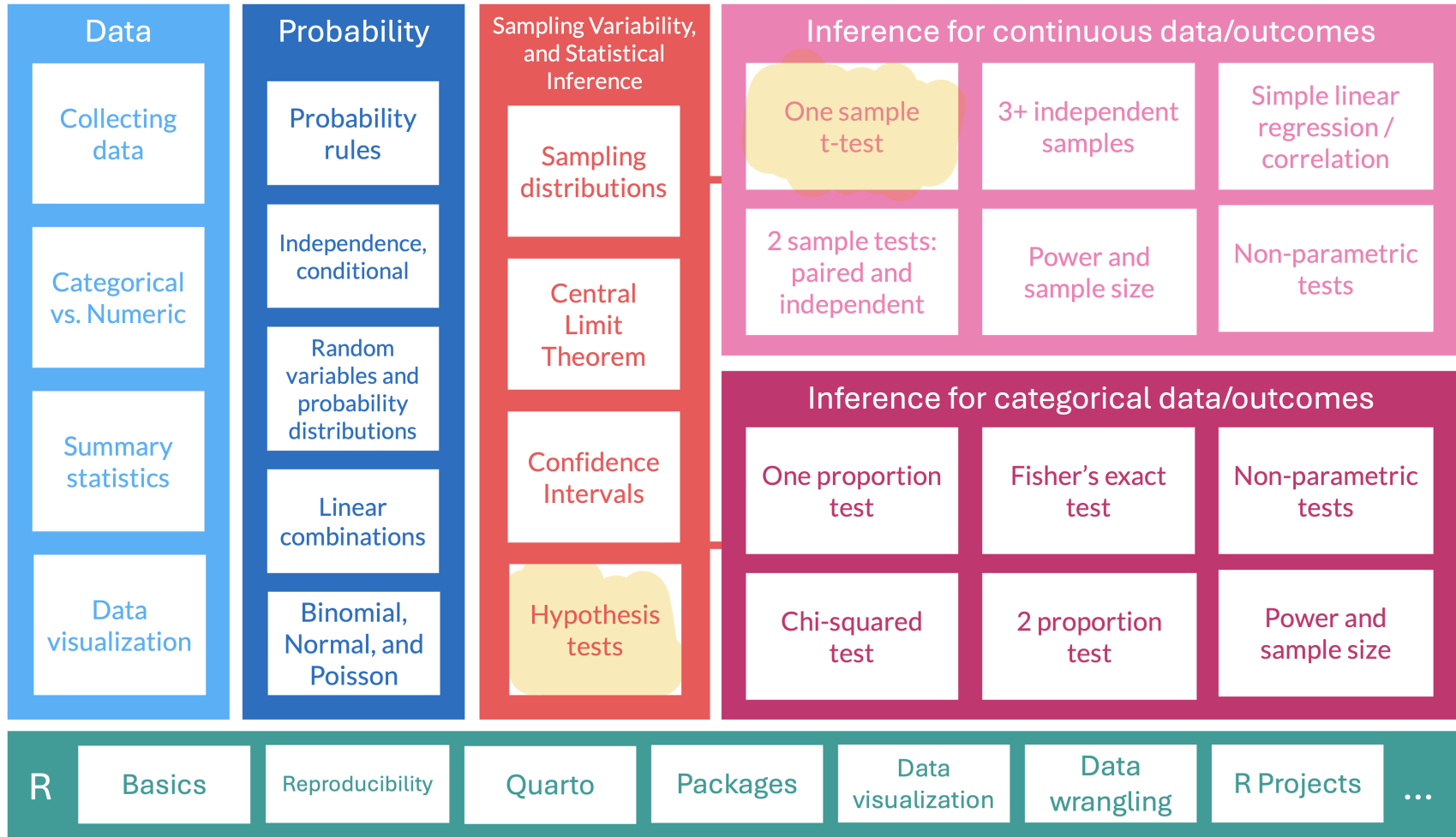
Meike Niederhausen and Nicky Wakim

2025-11-05

# Learning Objectives

1. Understand the relationship between point estimates, confidence intervals, and hypothesis tests.
2. Determine if a single-sample mean is different than a population mean using a hypothesis test.
3. Use R to calculate the test statistic, p-value, and confidence interval for a single-sample mean.

# Where are we?



# Hypothesis tests we will learn

CI's and hypothesis testing for different scenarios:

| Lesson | Section | Population parameter    | Symbol (pop)        | Point estimate             | Symbol (sample)         |
|--------|---------|-------------------------|---------------------|----------------------------|-------------------------|
| 12     | 5.1     | Pop mean                | $\mu$               | Sample mean                | $\bar{x}$               |
| 13     | 5.2     | Pop mean of paired diff | $\mu_d$ or $\delta$ | Sample mean of paired diff | $\bar{x}_d$             |
| 14     | 5.3     | Diff in pop means       | $\mu_1 - \mu_2$     | Diff in sample means       | $\bar{x}_1 - \bar{x}_2$ |
| 16     | 8.1     | Pop <u>proportion</u>   | $p$                 | Sample prop                | $\hat{p}$               |
| 16     | 8.2     | Diff in pop prop's      | $p_1 - p_2$         | Diff in sample prop's      | $\hat{p}_1 - \hat{p}_2$ |

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# Answering a research question with a single mean

Research question is a generic form: Is there evidence to support that the population mean is different than  $\mu_0$ ?

- $\mu_0$  is the generic form for a prescribed value:  $\mu$  is the population mean and we want to see if  $\mu = \mu_0$

$$\mu = \underbrace{98.6^\circ\text{F}}_{\mu_0}$$

Two approaches to answer this question:

## Confidence interval

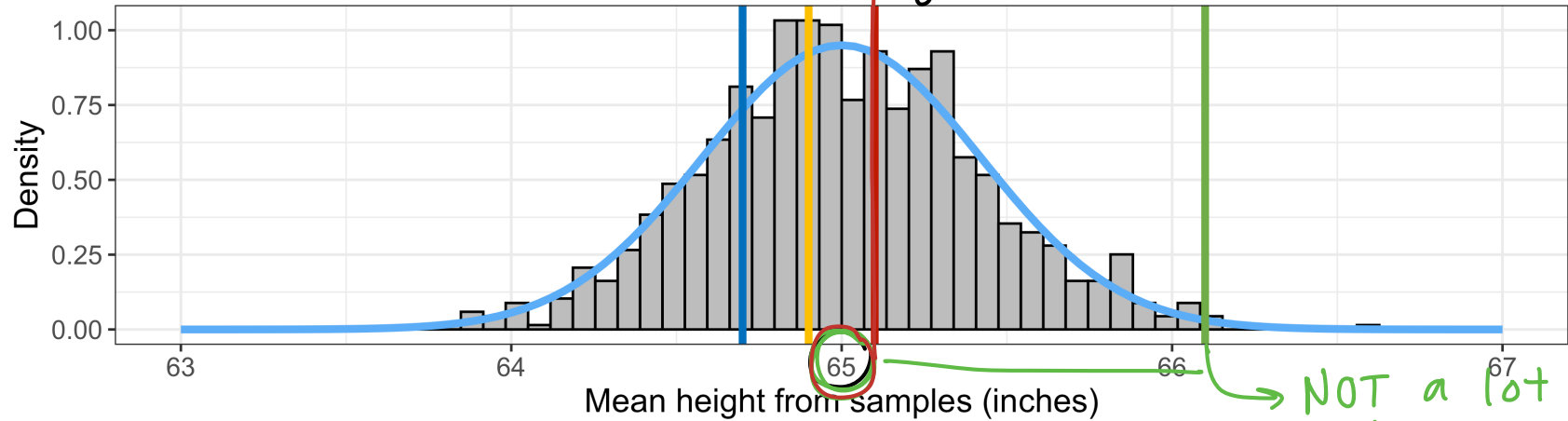
- Create a **confidence interval (CI)** for the population mean  $\mu$  from our sample data and determine whether a prescribed value ( $\mu_0$ ) is inside the CI or not
- Answering the question: is  $\mu_0$  a plausible value given our data?

- If CI does NOT contain  $\mu_0$  then the answer is **NO** "evidence to support population mean is different than  $\mu_0$ "

## Hypothesis test

- Run a **hypothesis test** to see if there is evidence that the population mean  $\mu$  is significantly different from a prescribed value ( $\mu_0$ ) **YES/NO**
- This does not give us a range of plausible values for the population mean  $\mu$ .
- Instead, we calculate a **test statistic** and **p-value**
- See how likely we are to observe the sample mean  $\bar{x}$  or a more extreme sample mean assuming that the population mean  $\mu$  is a prescribed value

# Last last time: Point estimates *sampling distribution*



Sample 50 people  
 $\bar{x} = 65.1, s = 2.8$

Sample 50 people  
 $\bar{x} = 64.7, s = 3.1$

Sample 50 people  
 $\bar{x} = 64.9, s = 3.2$

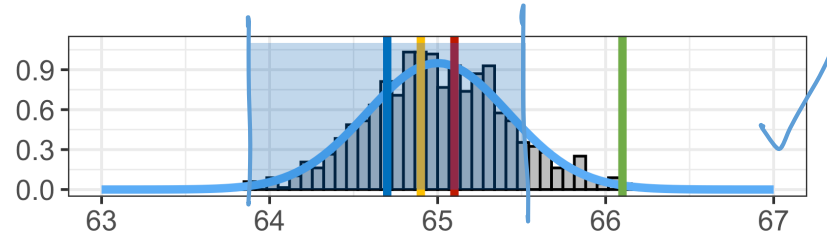
Sample 50 people  
 $\bar{x} = 66.1, s = 3.4$

*w/ mean 65*

$$\mu = 65 \text{ inches}$$

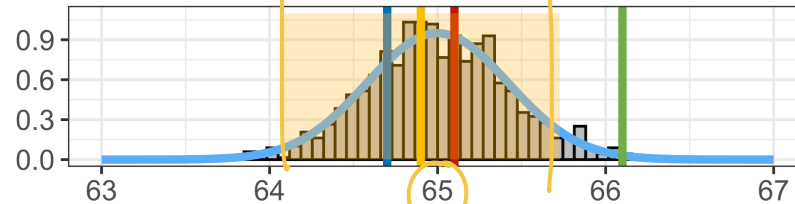
# Last time: Point estimates with their confidence intervals for $\mu$

Sample 50 people  
 $\bar{x} = 64.7, s = 3.1$

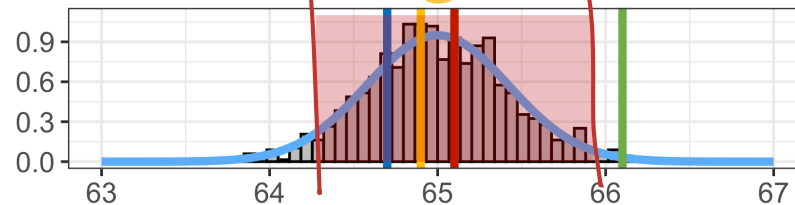


Do these confidence intervals  
include  $\mu$ ?  $\mu = 65$

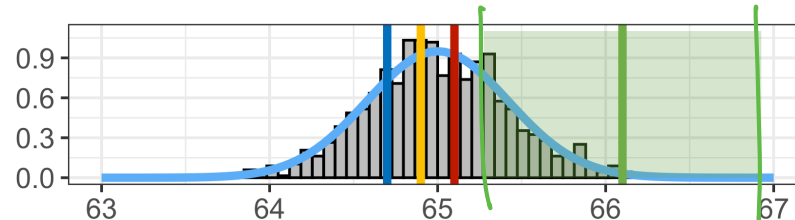
Sample 50 people  
 $\bar{x} = 64.9, s = 3.2$



Sample 50 people  
 $\bar{x} = 65.1, s = 2.8$



Sample 50 people  
 $\bar{x} = 66.1, s = 3.4$

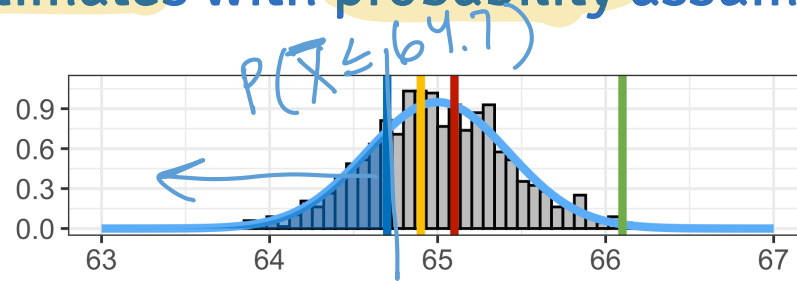


Research q:  
Do we think  
the pop mean  
height is  
65?

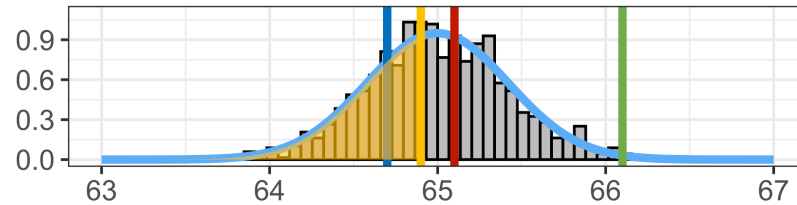
95% CI  $\Rightarrow$   
5% of samplers  
will say NO  
even though  
taken from pop

# This time: Point estimates with probability assuming population mean $\mu$

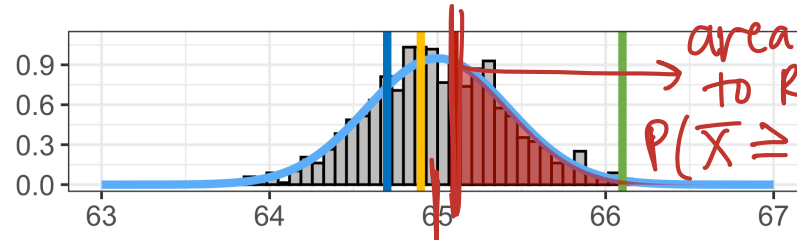
Sample 50 people  
 $\bar{x} = 64.7, s = 3.1$



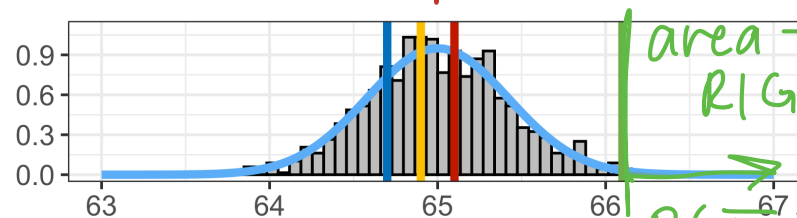
Sample 50 people  
 $\bar{x} = 64.9, s = 3.2$



Sample 50 people  
 $\bar{x} = 65.1, s = 2.8$



Sample 50 people  
 $\bar{x} = 66.1, s = 3.4$



Assuming the population mean is  $\mu$  (65 inches), what is the probability that we observe  $\bar{x}$  or a more extreme sample mean?

higher prob means more confident that sample 13 taken from pop w/ mean 65

$< 0.05$   
 $P(\bar{X} \geq 66.1) = \text{small}$   
 NOT confident

# Last time: Confidence interval (CI) for the mean $\mu$ ( $z$ vs. $t$ )

- In summary, we have two cases that lead to different ways to calculate the confidence interval

★ MORE COMMON

Case 1: We know the population standard deviation

$$\bar{x} \pm z^* \times SE$$

- with  $SE = \frac{\sigma}{\sqrt{n}}$  and  $\sigma$  is the population standard deviation
- For 95% CI, we use:
  - $z^* = \text{qnorm}(p = 0.975) = 1.96$

Case 2: We do not know the population sd

$$\bar{x} \pm t^* \times SE$$

- with  $SE = \frac{s}{\sqrt{n}}$  and  $s$  is the sample standard deviation
- For 95% CI, we use:
  - $t^* = \text{qt}(p = 0.975, df = n-1)$

$$(\bar{x} - t^* SE, \bar{x} + t^* SE)$$

is  $\mu_0$  w/in values?

# Poll Everywhere Question 1

13:35 Wed Nov 5



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*if said "pop mean", then correct*

Which of the following statements best describes a confidence interval for a population mean,  $\mu$ ?

A range that contains the exact population mean. 5%

A range of values we expect the sample mean to fall within. 29%

A range of plausible values for the population mean based on sample data. 67% ✓

A range that excludes all possible values of the population mean. 0%

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# This time: Hypothesis test ( $z$ vs. $t$ )

use test statistics to find prob

- We have two different distributions from which we run a hypothesis test

## Case 1: We know the population standard deviation

- We use a test statistic from a Normal distribution:

$$z_{\bar{x}} = \frac{\bar{x} - \mu}{SE}$$

- with  $SE = \frac{\sigma}{\sqrt{n}}$  and  $\sigma$  is the population standard deviation

## Case 2: We do not know the population sd

- We use a test statistic from a Student's  $t$ -distribution:

$$t_{\bar{x}} = \frac{\bar{x} - \mu}{SE}$$

- with  $SE = \frac{s}{\sqrt{n}}$  and  $s$  is the sample standard deviation

- This is usually the case in real life

# Is 98.6°F really the mean “healthy” body temperature?

- We will illustrate how to perform a hypothesis test as we work through this example
  - Where did the 98.6°F value come from?
    - German physician Carl Reinhold August Wunderlich determined 98.6°F (or 37°C) based on temperatures from 25,000 patients in Leipzig in 1851.
  - 1992 JAMA article by Mackowiak, Wasserman, & Levine
    - They claim that 98.2°F (36.8°C) is a more accurate average body temp
    - Sample: n = 148 healthy individuals aged 18 - 40 years
  - Other research indicating that the human body temperature is lower
    - *Decreasing human body temperature in the United States since the Industrial Revolution*
    - *Defining Usual Oral Temperature Ranges in Outpatients Using an Unsupervised Learning Algorithm*
    - NYT article *The Average Human Body Temperature Is Not 98.6 Degrees*
- considered pop mean*
- sample*

Question: based on the 1992 JAMA data, is there evidence to support that the population mean body temperature is different from 98.6°F?

# Question: based on the 1992 JAMA data, is there evidence to support that the population mean body temperature is different from 98.6°F?

Two approaches to answer this question:

## Confidence interval

- Create a **confidence interval (CI)** for the population mean  $\mu$  and determine whether 98.6°F is inside the CI or not.
- Answering the question: is 98.6°F a plausible value?

## Hypothesis test

- Run a **hypothesis test** to see if there is evidence that the population mean  $\mu$  is *significantly different* from 98.6°F or not
- This does not give us a range of plausible values for the population mean  $\mu$ .
- Instead, we calculate a *test statistic* and *p-value*
- See how likely we are to observe the sample mean  $\bar{x}$  or a more extreme sample mean assuming that the population mean  $\mu$  is 98.6°F

98.2°

# Approach 1: Create a 95% CI for the population mean body temperature

- Use data based on the results from the 1992 JAMA study
  - The original dataset used in the JAMA article is not available
  - However, Allen Shoemaker from Calvin College created a dataset with the same summary statistics as in the JAMA article, which we will use:

$$\bar{x} = 98.25, s = 0.733, n = 130$$

$$df = n - 1 = 130 - 1 = 129$$

$$\text{Used } t^* = qt(.975, df=129) = 1.979$$

based off of 95% CI

CI for  $\mu$ :

$$\begin{aligned} & \bar{x} \pm t^* \frac{s}{\sqrt{n}} \\ & 98.25 \pm 1.979 \cdot \frac{0.733}{\sqrt{130}} \\ & 98.25 \pm 0.127 \\ & (98.123, 98.377) \end{aligned}$$

**Conclusion:** We are 95% confident that the (population) mean body temperature is between 98.123°F and 98.377°F, which is discernably different than 98.6°F.

## Approach 2: Hypothesis Test

From before:

- Run a **hypothesis test** to see if there is evidence that the population mean  $\mu$  is significantly different from 98.6°F or not.
  - This does not give us a range of plausible values for the population mean  $\mu$ .
  - Instead, we calculate a *test statistic* and *p-value*
    - to see how likely we are to observe the sample mean  $\bar{x}$
    - or a more extreme sample mean
    - assuming that the population mean  $\mu$  is 98.6°F.

How do we calculate a *test statistic* and *p-value*?

- Use the sampling distribution and central limit theorem!!
- Focus on Case 2: we don't know the population sd  $\sigma$

↳ use  $t$ -distribution

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# General steps in a Hypothesis Test

1. Check the **assumptions**
2. Set the **level of significance**  $\alpha$
3. Specify the **null** ( $H_0$ ) and **alternative** ( $H_A$ ) **hypotheses**
  1. In symbols
  2. In words
  3. Alternative: one- or two-sided?
4. Calculate the **test statistic**.
5. Calculate the **p-value** based on the observed test statistic and its sampling distribution
6. Write a **conclusion** to the hypothesis test
  1. Do we reject or fail to reject  $H_0$ ?
  2. Write a conclusion in the context of the problem

# Step 1: Check the assumptions

- The assumptions to run a hypothesis test on a sample are:
  - **Independent observations**: the observations were collected independently.
  - **Approximately normal sample or big n**: the distribution of the sample should be approximately normal, or the sample size should be at least 30  $n > 30$ 
    - AKA: sample is approximately Normal OR we can use the CLT

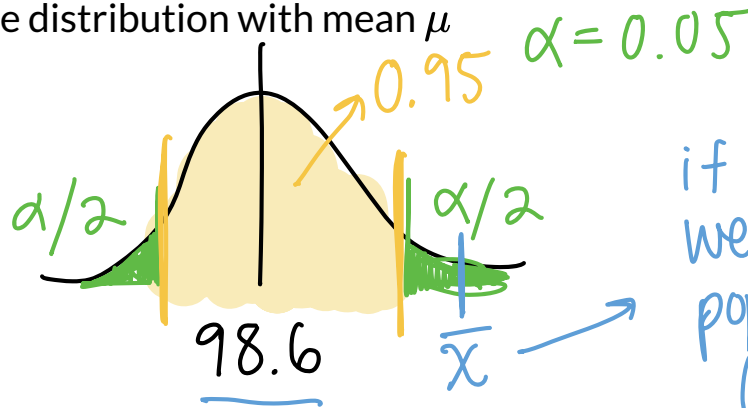
- These are the criteria for the Central Limit Theorem in Lesson <sup>10</sup>~~09~~: Variability in estimates

- In our example, we would check the assumptions with a statement:

- The individual observations are independent and the number of individuals in our sample is 130. Thus, we can use CLT to approximate the sampling distribution.

## Step 2: Set the level of significance $\alpha$

- Before doing a hypothesis test, we set a cut-off for how small the  $p$ -value should be in order to reject  $H_0$ .
- It is important to specify how rare or unlikely an event must be in order to represent sufficient evidence against the null hypothesis. (we think pop mean is  $\mu_0$ )
- We call this the **significance level**, denoted by the Greek symbol **alpha ( $\alpha$ )**
  - Typically choose  $\alpha = 0.05$
- This is parallel to our confidence interval
  - $\alpha$  is the probability of rejecting the null hypothesis when it is true (it's a measure of potential error)
    - Null: our initial assumption about the mean (in example,  $\mu = 98.6$ )
  - From repeated  $(1 - \alpha)\%$  confidence intervals, we will have about  $\alpha\%$  intervals that do not cover  $\mu$  even though they come from the distribution with mean  $\mu$



if  $\bar{x}$  is w/in  $\alpha$  region,  
we do not think  
pop mean is 98.6  
(reject null)

## Step 3: Null & Alternative Hypotheses (1/2)

In statistics, a **hypothesis** is a statement about the value of an **unknown population parameter**.

A **hypothesis test** consists of a test between two competing hypotheses:

1. a **null** hypothesis  $H_0$  (pronounced “H-naught”) vs.
2. an **alternative** hypothesis  $H_A$  (also denoted  $H_1$ )

Example of hypotheses in words:

$H_0$ : The population mean body temperature is 98.6° F  
vs.  $H_A$ : The population mean body temperature is not 98.6° F

$$\begin{array}{l} \mu = 98.6 \\ \hline \text{pop mean} \end{array} \text{ is } \frac{\quad}{98.6}$$

1.  $H_0$  is a claim that there is “no effect” or “no difference of interest.”
2.  $H_A$  is the claim a researcher wants to establish or find evidence to support. It is viewed as a “challenger” hypothesis to the null hypothesis  $H_0$

↳ need evidence to prove alternative

## Step 3: Null & Alternative Hypotheses (2/2)

### Notation for hypotheses

$$H_0 : \mu = \mu_0 \quad \text{prescribed value}$$

vs.  $H_A : \mu \neq, <, \text{ or }, > \mu_0$

### Hypotheses test for example

$$H_0 : \mu = 98.6$$

vs.  $H_A : \mu \neq 98.6$

*is not*

We call  $\mu_0$  the *null value* (hypothesized population mean from  $H_0$ )

$$H_A : \mu \neq \mu_0$$

- not choosing a priori whether we believe the population mean is greater or less than the null value  $\mu_0$

$$H_A : \mu < \mu_0$$

- believe the population mean is less than the null value  $\mu_0$
- less than 98.6°*


$$H_A : \mu > \mu_0$$

- $H_A : \mu \neq \mu_0$  is the most common option, since it's the most conservative

# Poll Everywhere Question 2

14:14 Wed Nov 5

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For testing if a population mean is greater than a specified value, which of the following correctly specifies the null and alternative hypotheses for a one-sided test?

$H_0 : \mu = \mu_0$  vs.  $H_A : \mu \neq \mu_0$  5% *two-sided test*

$H_0 : \mu = \mu_0$  vs.  $H_A : \mu > \mu_0$  95% ✓

$H_0 : \mu \neq \mu_0$  vs.  $H_A : \mu = \mu_0$  0%

$H_0 : \mu = \mu_0$  vs.  $H_A : \mu < \mu_0$  0%

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$$H_0 : \mu = \mu_0$$
$$\mu = 98.6$$

$$H_A : \mu > \mu_0$$
$$\mu > 98.6$$

## Step 4: Test statistic (& its distribution)

### Case 1: We know the population standard deviation

- We use a test statistic from a Normal distribution:

$$z_{\bar{x}} = \frac{\bar{x} - \mu}{SE}$$

- with  $SE = \frac{\sigma}{\sqrt{n}}$  and  $\sigma$  is the population standard deviation
- Statistical theory tells us that  $z_{\bar{x}}$  follows a **Standard Normal distribution**  $N(0, 1)$

### Case 2: We do not know the population sd

- We use test statistic from Student's t-distribution:

$$t_{\bar{x}} = \frac{\bar{x} - \mu}{SE}$$

- with  $SE = \frac{s}{\sqrt{n}}$  and  $s$  is the sample standard deviation
- Statistical theory tells us that  $t_{\bar{x}}$  follows a **Student's t distribution** with degrees of freedom (df) =  $n - 1$

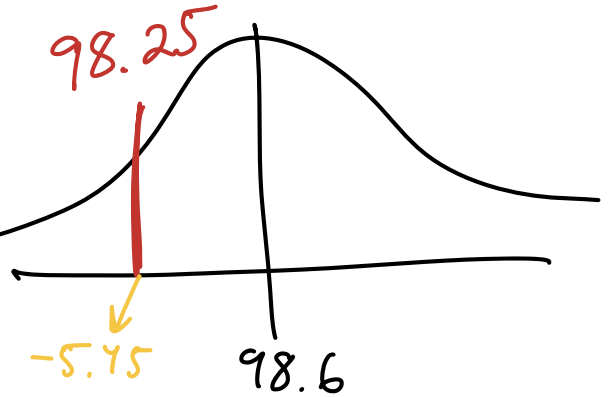
$\bar{x}$  = sample mean,  $\mu_0$  = hypothesized population mean from  $H_0$ ,  
 $\sigma$  = *population* standard deviation,  $s$  = *sample* standard deviation,  
 $n$  = sample size

## Step 4: Test statistic calculation

From our example: Recall that  $\bar{x} = 98.25$ ,  $s = 0.733$ , and  $n = 130$

The test statistic is:

$$t_{\bar{x}} = \frac{\bar{x} - \mu_0}{\frac{s}{\sqrt{n}}} = \frac{98.25 - 98.6}{\frac{0.73}{\sqrt{130}}} = -5.45$$



- Statistical theory tells us that  $t_{\bar{x}}$  follows a **Student's t-distribution** with  $df = n - 1 = 129$

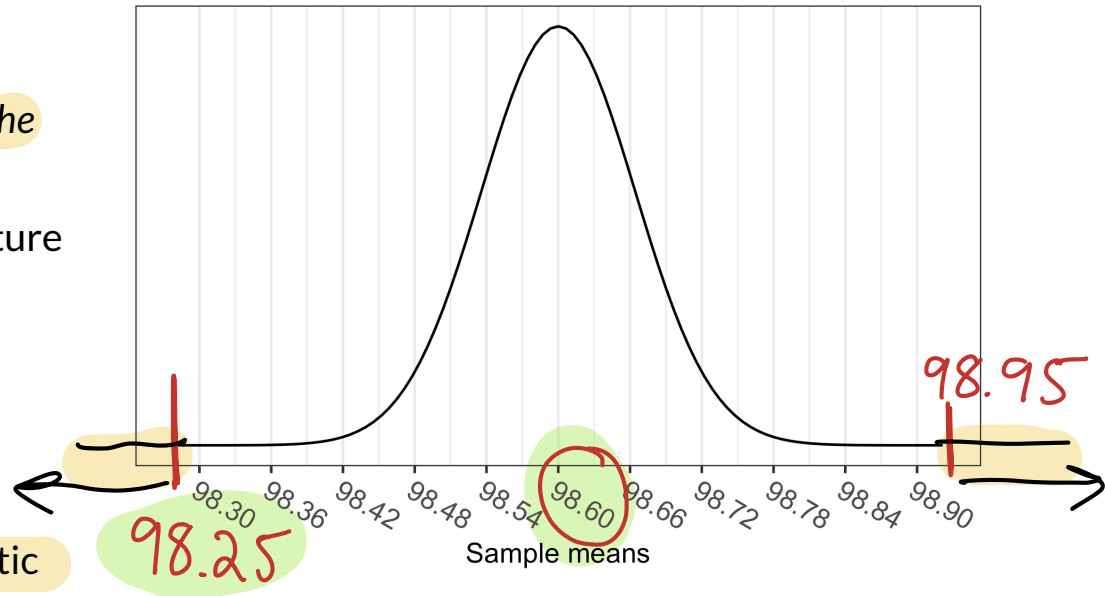


## Step 5: p-value

The **p-value** is the **probability** of obtaining a test statistic *just as extreme or more extreme* than the observed test statistic assuming the null hypothesis  $H_0$  is true.

- The  $p$ -value is a quantification of “surprise”
  - Assuming  $H_0$  is true, how surprised are we with the observed results?
  - Ex: assuming that the true mean body temperature is  $98.6^\circ\text{F}$ , how surprised are we to get a sample mean of  $98.25^\circ\text{F}$  (or more extreme)?
- If the  $p$ -value is “small,” it means there’s a small probability that we would get the observed statistic (or more extreme) when  $H_0$  is true.

*under the null*  
Sampling distribution of mean body temperatures



## Step 5: p-value calculation

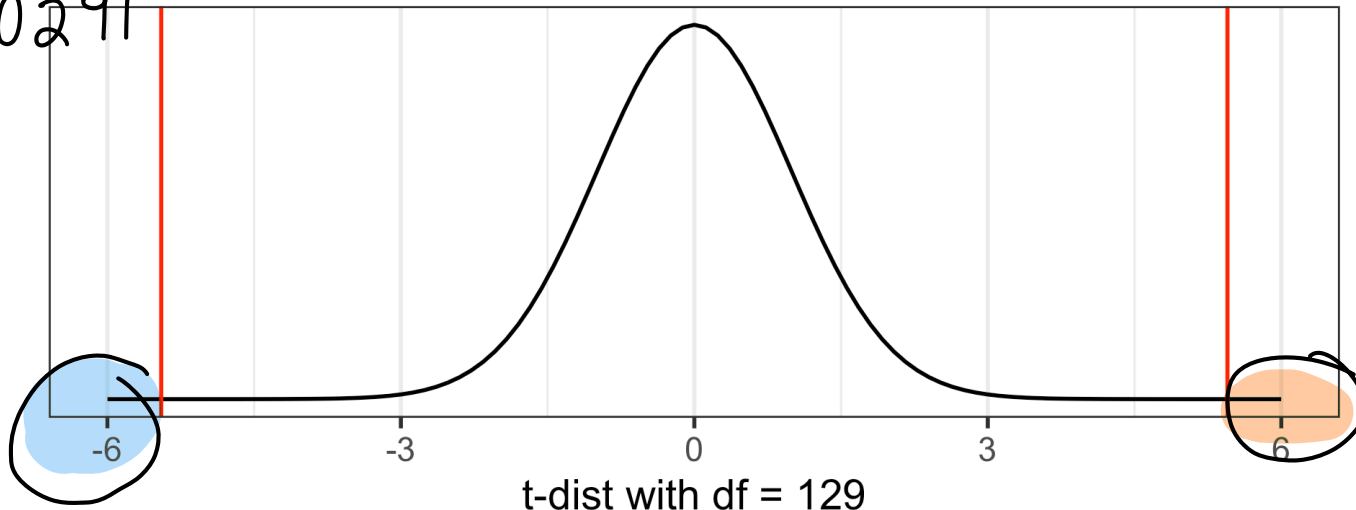
Calculate the  $p$ -value using the Student's  $t$ -distribution with  $df = n - 1 = 130 - 1 = 129$ :

$$p\text{-value} = P(T \leq -5.45) + P(T \geq 5.45) = 2.410889 \times 10^{-07}$$

```
1 # use pt() instead of pnorm()
2 # need to specify df
3 2*pt(-5.4548, df = 130-1, lower.tail = TRUE)
```

```
[1] 2.410889e-07
```

0.000000241



## Step 6: Conclusion to hypothesis test

$$\left. \begin{array}{l} H_0 : \mu = \mu_0 \\ \text{vs. } H_A : \mu \neq \mu_0 \end{array} \right\}$$

- Need to compare p-value to our selected  $\alpha = 0.05$
- Do we reject or fail to reject  $H_0$ ?

general forms:

If p-value  $< \alpha$ , reject the null hypothesis

- There is sufficient evidence that the (population) mean body temperature is discernibly different from  $\mu_0$  ( $p$ -value = \_\_)
- The average (insert measure) in the sample was  $\bar{x}$  (95% CI , ), which is discernibly different from  $\mu_0$  ( $p$ -value = \_\_).

If p-value  $\geq \alpha$ , fail to reject the null hypothesis

- There is insufficient evidence that the (population) mean body temperature is discernibly different from  $\mu_0$  ( $p$ -value = \_\_)
- The average (insert measure) in the sample was  $\bar{x}$  (95% CI , ), which is not discernibly different from  $\mu_0$  ( $p$ -value = \_\_).

more what we share w/ world

## Step 6: Conclusion to hypothesis test

$$H_0 : \mu = 98.6$$


vs.  $H_A : \mu \neq 98.6$

- Recall the  $p$ -value =  $2.410889 \times 10^{-07}$
- Need to compare back to our selected  $\alpha = 0.05$
- Do we reject or fail to reject  $H_0$ ?

$$0.000000241 < \alpha = 0.05$$

$\Rightarrow$  Reject

### Conclusion statement:

- Basic: (“stats class” conclusion)
  - There is sufficient evidence that the (population) mean body temperature is discernibly different from 98.6°F ( $p$ -value  $< 0.001$ ). 
- Better: (“manuscript style” conclusion)
  - The average body temperature in the sample was 98.25°F (95% CI 98.12, 98.38°F), which is discernibly different from 98.6°F ( $p$ -value  $< 0.001$ ).

# Poll Everywhere Question 3

14:33 Wed Nov 5

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A public health researcher tests if the average daily water intake in a community differs from the recommended 2 liters. The test yields a p-value of 0.08, with a significance level  $\alpha = 0.05$ . What should the researcher conclude?

- if pval <  $\alpha$*
- Reject  $H_0$ : There is sufficient evidence to conclude the average intake is different from 2 liters. 15%
  - Fail to reject  $H_0$ : There is insufficient evidence to conclude the average intake is different from 2 liters. 70% ✓
  - Accept  $H_0$ : There is insufficient evidence to conclude the average intake is different from 2 liters. 10%
  - Reject  $H_0$ : There is insufficient evidence to conclude the average intake is 2 liters. 5%

$$H_0: \mu = 2$$

$$H_A: \mu \neq 2$$

$$\alpha = 0.05$$

$$p\text{-value} = 0.08 > \alpha = 0.05$$

⇒ fail to reject

# Learning Objectives

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3. Use R to calculate the test statistic, p-value, and confidence interval for a single-sample mean.

# Load the dataset

- The data are in a csv file called `BodyTemperatures.csv`

```
1 library(here) # first install this package
2
3 BodyTemps <- read.csv(here::here("data", "BodyTemperatures.csv"))
4 #           location: look in "data" folder
5 #           for the file "BodyTemperatures.csv"
6
7 glimpse(BodyTemps)
```

Rows: 130

Columns: 3

\$ Temperature <dbl> 96.3, 96.7, 96.9, 97.0, 97.1, 97.1, 97.1, 97.2, 97.3, 97.4...

\$ Gender <int> 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1...

\$ HeartRate <int> 70, 71, 74, 80, 73, 75, 82, 64, 69, 70, 68, 72, 78, 70, 75...

# t.test: base R's function for testing one mean

- Use the body temperature example with  $H_A : \mu \neq 98.6$
- We called the dataset `BodyTemps` when we loaded it

```
1 (temps_ttest <- t.test(x = BodyTemps$Temperature,  
2 alternative = "two.sided", # default setting  
3 mu = 98.6))
```

"one.sided"  
< >

One Sample t-test

prescribed  
mean ( $\mu_0$ )

$H_A : \mu \neq 98.6$

data: BodyTemps\$Temperature

t = -5.4548, df = 129, p-value = 2.411e-07

alternative hypothesis: true mean is not equal to 98.6

95 percent confidence interval: → 95% CI  
98.12200 98.37646

sample estimates:

mean of x }  $\bar{x}$   
98.24923

Note that the test output also gives the 95% CI using the t-distribution.

# tidy() the t.test output

- Use the `tidy()` function from the `broom` package for briefer output in table format that's stored as a `tibble`
- Combined with the `gt()` function from the `gt` package, we get a nice table

```
1 tidy(temps_ttest) %>% } tidy() + gt(): makes results neater  
2   gt() %>%  
3   tab_options(table.font.size = 40) # use a different size in your HW
```

| $\bar{x}$ estimate | t-statistic | p.value      | parameter | conf.low | conf.high | method            | alternative |
|--------------------|-------------|--------------|-----------|----------|-----------|-------------------|-------------|
| 98.24923           | -5.454823   | 2.410632e-07 | 129       | 98.122   | 98.37646  | One Sample t-test | two.sided   |

- Since the `tidy()` output is a tibble, we can easily `pull()` specific values from it:

Using base R's `$`

```
1 tidy(temps_ttest)$p.value
```

```
[1] 2.410632e-07
```

# What's next?

CI's and hypothesis testing for different scenarios:

| Lesson | Section | Population parameter    | Symbol (pop)        | Point estimate             | Symbol (sample)         |
|--------|---------|-------------------------|---------------------|----------------------------|-------------------------|
| ✓ 12   | 5.1     | Pop mean                | $\mu$               | Sample mean                | $\bar{x}$               |
| 13     | 5.2     | Pop mean of paired diff | $\mu_d$ or $\delta$ | Sample mean of paired diff | $\bar{x}_d$             |
| 14     | 5.3     | Diff in pop means       | $\mu_1 - \mu_2$     | Diff in sample means       | $\bar{x}_1 - \bar{x}_2$ |
| 16     | 8.1     | Pop proportion          | $p$                 | Sample prop                | $\hat{p}$               |
| 16     | 8.2     | Diff in pop prop's      | $p_1 - p_2$         | Diff in sample prop's      | $\hat{p}_1 - \hat{p}_2$ |

# Reference: what does it all look like together?

Example of hypothesis test based on the 1992 JAMA data

Is there evidence to support that the population mean body temperature is different from 98.6°F?

1. **Assumptions:** The individual observations are independent and the number of individuals in our sample is 130. Thus, we can use CLT to approximate the sampling distribution.

2. Set  $\alpha = 0.05$

3. **Hypothesis:**

$$H_0 : \mu = 98.6$$

$$\text{vs. } H_A : \mu \neq 98.6$$

4-5.

```
1 temps_ttest <- t.test(x = BodyTemps$Temperature, mu = 98.6)
2 tidy(temps_ttest) %>% gt() %>% tab_options(table.font.size = 36)
```

| estimate | statistic | p.value      | parameter | conf.low | conf.high | method            | alternative |
|----------|-----------|--------------|-----------|----------|-----------|-------------------|-------------|
| 98.24923 | -5.454823 | 2.410632e-07 | 129       | 98.122   | 98.37646  | One Sample t-test | two.sided   |

6. **Conclusion:** We reject the null hypothesis. The average body temperature in the sample was 98.25°F (95% CI 98.12, 98.38°F), which is discernibly different from 98.6°F ( $p$ -value < 0.001).